Models for Predicting Financial Distress: Z-Score After 50 Years, What Have We Learned?

Dr. Edward Altman NYU Stern School of Business

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Sessions 1 & 2



Scoring Systems

- Qualitative (Subjective) 1800s
- Univariate (Accounting/Market Measures)
 - Rating Agency (e.g. *Moody's* (1909), *S&P Global Ratings* (1916) and Corporate (e.g., *DuPont*) Systems (early 1900s)
- Multivariate (Accounting/Market Measures) -1968 (Z-Score) \rightarrow Present
 - Discriminant, Logit, Probit Models (Linear, Quadratic)
 - Non-Linear and "Black-Box" Models (e.g., Recursive Partitioning, Neural Networks, 1990s), Machine Learning, Hybrid
- Discriminant and Logit Models in Use for
 - Consumer Models Fair Isaacs (FICO Scores)
 - Manufacturing Firms (1968) Z-Scores
 - Extensions and Innovations for Specific Industries and Countries (1970s Present)
 - ZETA Score Industrials (1977)
 - Private Firm Models (e.g., Z'-Score (1983), Z"-Score (1995))
 - EM Score Emerging Markets (1995)
 - Bank Specialized Systems (1990s)
 - SMEs (e.g. Edmister (1972), Altman & Sabato (2007) & Wiserfunding (2016))
- Option/Contingent Claims Models (1970s Present)
 - Risk of Ruin (Wilcox, 1973)
 - KMVs Credit Monitor Model (1993) Extensions of Merton (1974) Structural Framework



Scoring Systems (continued)

- Artificial Intelligence Systems (1990s Present)
 - Expert Systems
 - Neural Networks
 - Machine Learning
- Blended Ratio/Market Value/Macro/Governance/Invoice Data Models
 - Altman Z-Score (Fundamental Ratios and Market Values) 1968
 - Bond Score (Credit Sights, 2000; RiskCalc Moody's, 2000)
 - Hazard (Shumway), 2001)
 - Kamakura's Reduced Form, Term Structure Model (2002)
 - Z-Metrics (Altman, et al, *Risk Metrics*[®], 2010)
- Re-introduction of Qualitative Factors/FinTech
 - Stand-alone Metrics, e.g., Invoices, Payment History
 - Multiple Factors Data Mining (Big Data Payments, Governance, time spent on individual firm reports [e.g., *CreditRiskMonitor's* revised FRISK Scores, 2017], etc.)



Major Agencies Bond Rating Categories

Moody's		S&P/Fitch	
Aaa Aa1 Aa2 Aa3 A1 A2 A3 Baa1 Baa2	Investment	AAA AA+ AA AA- A+ A A- BBB+ BBB	
Baas Baas Baas Baas Baas Baas Baas	High Yield ("Junk")	BBB- BB- B+	
B2 B3 Caa1 Caa Caa3		B B- CCC+ CCC CCC-	High Yield Market
C	Ļ	C D	

Z-Score (1968) Component Definitions and Weightings

Variable	Definition	Weighting Factor
X ₁ 	Working Capital	1.2
	Total Assets	
X ₂	Retained Earnings	1.4
	Total Assets	
X ₃	EBIT	3.3
	Total Assets	
X ₄	Market Value of Equity	0.6
	Book Value of Total Liabilit	ies
X ₅	Sales	1.0
	Total Assets	5



Zones of Discrimination: Original Z - Score Model (1968)



Time Series Impact On Corporate Z-Scores

- Credit Risk Migration
 - Greater Use of Leverage
 - Impact of HY Bond & Lev Loan Markets
 - Global Competition
 - More and Larger Bankruptcies
 - Near Extinction of U.S. AAA Firms
- Increased Type II Error

The Near Extinction of the U.S. AAA Rated Company



Number of AAA Rated Groups in the U.S.

Sources: Standard & Poor's, Estimated from Platt, E., "Triple A Quality Fades as Companies Embrace Debt", Financial Times, May 24, 2016.



Estimating Probability of Default (PD) and Probability of Loss Given Defaults (LGD)

Method #1

- Credit scores on new or existing debt
- Bond rating equivalents on new issues (Mortality) or existing issues (Rating Agency Cumulative Defaults)
- Utilizing mortality or cumulative default rates to estimate marginal and cumulative defaults
- Estimating Default Recoveries and Probability of Loss

or

Method #2

- Credit scores on new or existing debt
- Direct estimation of the probability of default
- Based on PDs, assign a rating

Median Z-Score by S&P Bond Rating for U.S. Manufacturing Firms: 1992 - 2017

Rating	2017 (No.)	2013 (No.)	2004-2010	1996-2001	1992-1995
AAA/AA	4.20 (14)	4.13 (15)	4.18	6.20*	4.80*
Α	3.85 (55)	4.00 (64)	3.71	4.22	3.87
BBB	3.10 (137)	3.01 (131)	3.26	3.74	2.75
BB	2.45 (173)	2.69 (119)	2.48	2.81	2.25
В	1.65 (94)	1.66 (80)	1.74	1.80	1.87
CCC/CC	0.73 (4)	0.23 (3)	0.46	0.33	0.40
D	-0.10 (6) ¹	$0.01 (33)^2$	-0.04	-0.20	0.05

*AAA Only.

¹ From 1/2014-11/2017, ²From 1/2011-12/2013.

Sources: S&P Global Market Intelligence's *Compustat* Database, mainly S&P 500 firms, compilation by NYU Salomon Center, Stern School of Business.



Marginal and Cumulative Mortality Rate Actuarial Approach

 $\mathbf{MMR}_{(\mathbf{r},\mathbf{t})} = \frac{\text{total value of defaulting debt from rating (r) in year (t)}}{\text{total value of the population at the start of the year (t)}}$ $\mathbf{MMR} = \mathbf{Marginal Mortality Rate}$

One can measure the cumulative mortality rate (CMR) over a specific time period (1,2,..., T years) by subtracting the product of the surviving populations of each of the previous years from one (1.0), that is,

$$CMR_{(r,t)} = 1 - \Pi SR_{(r,t)},$$

$$t = 1 \rightarrow N$$

$$r = AAA \rightarrow CCC$$

here $CMR_{(r,t)} = Cumulative Mortality Rate of (r) in (t),$

SR (r,t) = Survival Rate in (r,t), 1 - MMR (r,t)



Mortality Rates by Original Rating

All Rated Corporate Bonds* 1971-2017

		1	2	3	4	5	6	7	8	9	10
AAA	Marginal	0.00%	0.00%	0.00%	0.00%	0.01%	0.02%	0.01%	0.00%	0.00%	0.00%
	Cumulative	0.00%	0.00%	0.00%	0.00%	0.01%	0.03%	0.04%	0.04%	0.04%	0.04%
AA	Marginal	0.00%	0.00%	0.19%	0.05%	0.02%	0.01%	0.01%	0.01%	0.01%	0.01%
	Cumulative	0.00%	0.00%	0.19%	0.24%	0.26%	0.27%	0.28%	0.29%	0.30%	0.31%
Α	Marginal	0.01%	0.03%	0.10%	0.11%	0.08%	0.04%	0.02%	0.23%	0.06%	0.03%
	Cumulative	0.01%	0.04%	0.14%	0.25%	0.33%	0.37%	0.39%	0.62%	0.68%	0.71%
BBB	Marginal	0.31%	2.34%	1.23%	0.97%	0.48%	0.21%	0.24%	0.15%	0.16%	0.32%
	Cumulative	0.31%	2.64%	3.84%	4.77%	5.23%	5.43%	5.66%	5.80%	5.95%	6.25%
BB	Marginal	0.91%	2.03%	3.83%	1.96%	2.40%	1.54%	1.43%	1.08%	1.40%	3.09%
	Cumulative	0.91%	2.92%	6.64%	8.47%	10.67%	12.04%	13.30%	14.24%	15.44%	18.05%
В	Marginal	2.85%	7.65%	7.72%	7.74%	5.72%	4.45%	3.60%	2.04%	1.71%	0.73%
	Cumulative	2.85%	10.28%	17.21%	23.62%	27.99%	31.19%	33.67%	35.02%	36.13%	36.60%
222	Marginal	8.09%	12.40%	17.71%	16.22%	4.88%	11.60%	5.39%	4.73%	0.62%	4.23%
	Cumulative	8.09%	19.49%	33.75%	44.49%	47.20%	53.33%	55.84%	57.93%	58.19%	59.96%

Years After Issuance

*Rated by S&P at Issuance Based on 3,359 issues

Source: S&P Global Ratings and Author's Compilation



Mortality Losses by Original Rating

All Rated Corporate Bonds* 1971-2017

		1	2	3	4	5	6	7	8	9	10
AAA	Marginal	0.00%	0.00%	0.00%	0.00%	0.01%	0.01%	0.01%	0.00%	0.00%	0.00%
	Cumulative	0.00%	0.00%	0.00%	0.00%	0.01%	0.02%	0.03%	0.03%	0.03%	0.03%
AA	Marginal	0.00%	0.00%	0.02%	0.02%	0.01%	0.01%	0.00%	0.01%	0.01%	0.01%
	Cumulative	0.00%	0.00%	0.02%	0.04%	0.05%	0.06%	0.06%	0.07%	0.08%	0.09%
Α	Marginal	0.00%	0.01%	0.04%	0.04%	0.05%	0.04%	0.02%	0.01%	0.05%	0.02%
	Cumulative	0.00%	0.01%	0.05%	0.09%	0.14%	0.18%	0.20%	0.21%	0.26%	0.28%
BBB	Marginal	0.22%	1.51%	0.70%	0.57%	0.25%	0.15%	0.09%	0.08%	0.09%	0.17%
	Cumulative	0.22%	1.73%	2.41%	2.97%	3.21%	3.36%	3.45%	3.52%	3.61%	3.77%
BB	Marginal	0.54%	1.16%	2.28%	1.10%	1.37%	0.74%	0.77%	0.47%	0.72%	1.07%
	Cumulative	0.54%	1.69%	3.94%	4.99%	6.29%	6.99%	7.70%	8.14%	8.80%	9.77%
В	Marginal	1.90%	5.36%	5.30%	5.19%	3.77%	2.43%	2.33%	1.11%	0.90%	0.52%
	Cumulative	1.90%	7.16%	12.08%	16.64%	19.78%	21.73%	23.56%	24.41%	25.09%	25.48%
CCC	Marginal	5.35%	8.67%	12.48%	11.43%	3.40%	8.60%	2.30%	3.32%	0.38%	2.69%
	Cumulative	5.35%	13.56%	24.34%	32.99%	35.27%	40.84%	42.20%	44.12%	44.33%	45.83%

Years After Issuance

*Rated by S&P at Issuance Based on 2,797 issues

Source: S&P Global Ratings and Author's Compilation



Financial Distress (Z-Score) Prediction Applications

External (To The Firm) Analytics

- Lenders (e.g., Pricing, Basel Capital Allocation)
- Bond Investors (e.g., Quality Junk Portfolio
- Long/Short Investment Strategy on Stocks (e.g. Baskets of Strong Balance Sheet Companies & Indexes, e.g. STOXX, Goldman, Nomura)
- Security Analysts & Rating Agencies
- Regulators & Government Agencies
- Auditors (Audit Risk Model) Going Concern
- Advisors (e.g., Assessing Client's Health)
- M&A (e.g., Bottom Fishing)

Internal (To The Firm) & Research Analytics

- To File or Not (e.g., General Motors)
- Comparative Risk Profiles Over Time
- Industrial Sector Assessment (e.g., Energy)
- Sovereign Default Risk Assessment
- Purchasers, Suppliers Assessment
- Accounts Receivables Management
- Researchers Scholarly Studies
- Chapter 22 Assessment
- Managers Managing a Financial Turnaround







IBM Corporation Z Score (1980 – 2001, update 2015-2017)



Year



Z-Score Model Applied to General Motors (Consolidated Data): Bond Rating Equivalents and Scores from 2005 – 2017

	Z-Scores	BRE
12/31/17	0.99	B-/CCC+
12/31/16	1.19	B-
12/31/15	1.30	B-
12/31/14	1.41	В
12/31/13	1.52	В
12/31/12	1.49	В
12/31/11	1.59	В
12/31/10	1.56	В
12/31/09	0.28	CCC
03/31/09	(1.12)	D
12/31/08	(0.63)	D
12/31/07	0.77	CCC+
12/31/06	1.12	B-
12/31/05	0.96	CCC+

Note: Consolidated Annual Results. Data Source: S&P Global Market Intelligence's S&P Capital IQ platform, Bloomberg., Edgar



Z-Score Model Applied to GM (Consolidated Data): Bond Rating Equivalents and Scores from 2005 – 2017



Z- Score: General Motors Co.



Additional Altman Z-Score Models:

Private Firm Model (1968)

Non-U.S., Emerging Markets Models for Non Financial Industrial Firms (1995) e.g. Latin America (1977, 1995), China (2010), etc.

Sovereign Risk Bottom-Up Model (2011)

SME Models for the U.S. (2007) & Europe

e.g. Italian Minibonds (2016), U.K. (2017), Spain (2018)



Italian High-Yield Bond Market

Our Work with U.S. H.Y. Bond Market, Classis Capital, Italian Borsa, & Wiserfunding

Providing a Credit Market Discipline to the Italian Mini-bond Market

Models to Assess the Risk & Return Trade-Off for Investors & Issuers of Mini-bonds



SME Z_I-Score: Summary of Results

- We segmented the Italian SMEs by industrial sectors and developed four default prediction models for Manufacturing, Services, Retail and Real Estate firms.
- Models have been developed on a representative sample of more the 14.500 SMEs located in the north of Italy and then certified for their relevance at national level.
- Prediction power of the models is significantly high due to the use of informative variables and appropriate techniques applied.
- In addition to the Score, Firms/Analysts/Investors also receive an estimated
 Bond Rating Equivalent and Probability of Default.
- ➤ The SME Z_I-Score improves the matching of demand and supply in the capital markets between SMEs looking for funding options and investors.



The Results

	Type I error	Type II error	1- Average	Accuracy
	rate	rate	Error Rate	ratio
Manufacturing Model	6.92%	26.57%	83.26%	93.08%
	(8.23%)	(27.64%)	(82.07%)	(92.21%)
Retail Model	16.77%	27.78%	77.73%	83.23%
	(18.54%)	(28.89%)	(76.29%)	(81.76%)
Services Model	12.05%	24.54%	81.70%	87.94%
	(14.88%)	(26.43%)	(79.35%)	(84.12%)
Constructions and Real	8.89%	26.02%	82.55%	91.11%
Estate	(10.12%)	(28.24%)	(80.82%)	(89.86%)



Risk Profile of Mini-bond issuers (2015)

Bond Rating Equivalent	# SMEs	% SMEs	Avg. Coupon Yield
AA	2	2%	0,057
A	4	4%	0,062
BBB	24	25%	0,065
BB	18	19%	0,055
В	31	32%	0,059
CCC	14	14%	0,065
CC	2	2%	0,030
С	2	2%	0,060

Source: Firms listed on Borsa Italiana Extra MOT, calculations by the authors



Source: Firms listed on Borsa Italiana Extra MOT, calculations by the authors

Applying our SME Z_I-Score on the mini-bond issuers as of 2015, we find that:

- Risk profile of SMEs doesn't seem to influence the bond pricing;
- Majority of existing minibond issuers classified as non-investment grade;
- The risk profile of the mini-bond issuers is better (i.e. less risky) than total SME sample.

Z" Score Model for Manufacturers, Non-Manufacturer Industrials; Developed and Emerging Market Credits (1995)

 $Z'' = 3.25 + 6.56X_1 + 3.26X_2 + 6.72X_3 + 1.05X_4$

 X_1 = Current Assets - Current Liabilities

Total Assets

 $X_2 =$ Retained Earnings

Total Assets

 X_3 = Earnings Before Interest and Taxes

Total Assets

 $X_4 =$ Book Value of Equity

Total Liabilities



US Bond Rating Equivalents Based on Z"-Score Model

Z"=3.25+6.56X ₁ +3.26X ₂ +6.72X ₃ +1.05X ₄						
Rating	Median 1996 Z"-Score ^a	Median 2006 Z"-Score ^a	Median 2013 Z"-Score ^a			
AAA/AA+	8.15 (8)	7.51 (14)	8.80 (15)			
AA/AA-	7.16 (33)	7.78 (20)	8.40 (17)			
A+	6.85 (24)	7.76 (26)	8.22 (23)			
A	6.65 (42)	7.53 (61)	6.94 (48)			
A-	6.40 (38)	7.10 (65)	6.12 (52)			
BBB+	6.25 (38)	6.47 (74)	5.80 (70)			
BBB	5.85 (59)	6.41 (99)	5.75 (127)			
BBB-	5.65 (52)	6.36 (76)	5.70 (96)			
BB+	5.25 (34)	6.25 (68)	5.65 (71)			
BB	4.95 (25)	6.17 (114)	5.52 (100)			
BB-	4.75 (65)	5.65 (173)	5.07 (121)			
B+	4.50 (78)	5.05 (164)	4.81 (93)			
В	4.15 (115)	4.29 (139)	4.03 (100)			
B-	3.75 (95)	3.68 (62)	3.74 (37)			
CCC+	3.20 (23)	2.98 (16)	2.84 (13)			
CCC	2.50 (10)	2.20 (8)	2.57(3)			
CCC-	1.75 (6)	1.62 (-) ^b	1.72 (-) ^b			
CC/D	0 (14)	0.84 (120)	0.05 (94) ^c			
			25			

^aSample Size in Parantheses. ^bInterpolated between CCC and CC/D. ^cBased on 94 Chapter 11 bankruptcy filings, 2010-2013. Sources: Compustat, Company Filings and S&P.

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Z and Z"-Score Models Applied to Sears, Roebuck & Co.: Bond Rating Equivalents and Scores from 2014 – 2017

Z and Z"- Score: Sears, Roebuck & Co.



Source: E. Altman, NYU Salomon Center



Tesla Z Scores and BREs (2014 – April 2018)



As of 12/31/2014 As of 12/31/2015 As of 12/31/2016 As of 12/31/2017 As of 4/23/2018



MANAGING A FINANCIAL TURNAROUND: APPLICATIONS OF THE Z-SCORE MODEL

THE GTI CASE



Financial Distress (Z-Score) Prediction Applications

External (To The Firm) Analytics

- Lenders (e.g., Pricing, Basel Capital Allocation)
- Bond Investors (e.g., Quality Junk Portfolio
- Long/Short Investment Strategy on Stocks (e.g. Baskets of Strong Balance Sheet Companies & Indexes, e.g. STOXX, Goldman, Nomura)
- Security Analysts & Rating Agencies
- Regulators & Government Agencies
- Auditors (Audit Risk Model) Going Concern
- Advisors (e.g., Assessing Client's Health)
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Internal (To The Firm) & Research Analytics

- To File or Not (e.g., General Motors)
- Comparative Risk Profiles Over Time
- Industrial Sector Assessment (e.g., Energy)
- Sovereign Default Risk Assessment
- Purchasers, Suppliers Assessment
- Accounts Receivables Management
- Researchers Scholarly Studies
- Chapter 22 Assessment
- Managers Managing a Financial Turnaround

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QUALITY JUNK STRATEGY



Return/Risk Tradeoffs – Distressed & High-Yield Bonds



Z" = 3.25 + 6.56X1 + 3.26X2 + 6.72X3 + 1.05X4 X1 = CA – CL / TA; X2 = RE / TA; X3 = EBIT / TA; X4 = BVE / TL

- **A** = Very High Return **/** Low Risk
- **B** = High Return **/** Low Risk
- **C** = Very High Return **/** High Risk
- **D** = High Return **/** High Risk



Objectives

- To demonstrate that specific management tools which work are available in crisis situations
- To illustrate that predictive models can be turned "inside out" and used as internal management tools to, in effect, reverse their predictions
- To illustrate an interactive, as opposed to a passive, approach to financial decision making

Physical Facilities & Financial Situation

- 7 Manufacturing facilities (California to New York)
- 3 Offices locations (California to Germany)
- American Stock Exchange Listed Company
- Incorporated in late 1960's
- Successful IPO through early 1970's



Financial Changes at GTI

- Working Capital decreased by \$6 million
- Retained Earnings decreased by \$2 million
- A \$2 million loss incurred
- Net Worth decreased from \$6,207 to \$4,370
- Market Value of Equity decreased by 50%
- Sales decreased by 50%



Ethical Consideration

- Pressure led to "Corner Cutting"
- Returns not reported
- Bad inventory (and too much of it)
- Questionable Deferrals and Reserves levels



- Internally Competitive
- Angry
- Insecure



• "PROTECT and ENHANCE the Stockholders Investment in GTI" (Words of the new CEO)



Material to be Covered

- Condition of GTI in June of 1975
- Management & Control changes
- Definition of Management's Responsibility
- Description of Management tools used
- Caveats for a successful Turnaround



Z-Score Component Definitions

<u>Variable</u>	Definition	Weighting Factor
\mathbf{X}_1	Working Capital Total Assets	1.2
X_2	Retained Earnings Total Assets	1.4
X ₃	EBIT Total Assets	3.3
X_4	Market Value of Equity Book Value of Total Liabilities	0.6
X_5	Sales Total Assets	.999
		39

Z-Score Distressed Firm Predictor: Application to GTI Corporation (1972 – 1975)





Components of Z-Score Distressed Firm: Predictor as Applied to GTI Corporation





Z-Score Distressed Firm Predictor: Application to GTI Corporation (1972 – 1975)





Management Tools Used

- Altman's Distressed Firm Predictor (Z-Score)
- Function / Location Matrix
- Financial Statements
- Planning Systems
- Trend Charts





- **Strategy #1**: Reduce Personnel & Eliminate Capital Spending
- Reason: Reverse Cash drain
- **Tool**: Source and Application of Funds
- **Timing**: Immediate



	Pennsylvania	Indiana	New York	California	West Germany	
Operations	\$1	\$1	\$1	\$1	\$1	\$5
Marketing	\$1	\$1	\$1	\$1	\$1	\$5
Engineering	\$1	\$1	\$1	\$1	\$1	\$5
Finance	\$1	\$1	\$1	\$1	\$1	\$5
	\$4	\$4	. \$4	\$4	\$4	\$20



• Immediate Reduction of Personnel

• Stop Capital Spending

Consolidate Profitable Product Lines



<u>Variable</u>	Definition	Weighting Factor
\mathbf{X}_1	Working Capital Total Assets	1.2
X_2	Retained Earnings Total Assets	1.4
X ₃	EBIT Total Assets	3.3
X_4	Market Value of Equity Book Value of Total Liabilities	0.6
X ₅	Sales Total Assets	.999
		47

Managerial & Financial Restructuring Actions and Impact on Z-Score

Strategy	<u>Reason</u>	<u>Impact</u>
Consolidated Locations	Eliminate Underutilized Assets	Z-Score
Drop Losing Product Lines	Eliminate Unprofitable Underutilized Assets	Z-Score
Reduce Debt Using Funds Received from Sale of Assets	Reduce Liabilities and Total Assets	Z-Score



Z-Score Distressed Firm Predictor Application to GTI Corporation (1972 – 1984)





Components of Z-Score Distressed Firm: Predictor as Applied to GTI Corporation









Sales Dollars / Employee



